## Section 1.4: BASIC RULES OF ALGEBRA

When you are done with your homework you should be able to...
$\pi$ Understand and use the vocabulary of algebraic expressions
$\pi$ Use commutative properties
$\pi$ Use associative properties
$\pi$ Use distributive properties
$\pi$ Combine like terms
$\pi$ Simplify algebraic expressions
WARM-UP:
Perform the indicated operation and simplify:

1. $\frac{57}{4} \div \frac{3}{2}$
2. $\frac{3}{14}-\frac{1}{10}$

## VOCABULARY OF ALGEBRAIC EXPRESSIONS

Terms: The $\qquad$ of an $\qquad$ expression are those parts that are $\qquad$ by $\qquad$ or $\qquad$ . A
$\qquad$ is a $\qquad$ a $\qquad$ or a
$\qquad$ What is the coefficient of a term which only has variables?

Constant term: A term that consists of just a $\qquad$ is called a

Like terms: Terms that have the $\qquad$ the $\qquad$
are called $\qquad$
Are constant terms like terms?

Example 1: Consider the following algebraic expression: $-12 x+9+7 x-8$

1. How many terms are there in the algebraic expression?
2. What is the coefficient of the first term?
3. List the constant term(s):
4. What are the like terms in the algebraic expression?

## EQUIVALENT ALGEBRAIC EXPRESSIONS

Two $\qquad$ expressions that have the $\qquad$ value for $\qquad$ replacements are called $\qquad$
$\qquad$
$\qquad$ ـ.

Example 2: Evaluate the following two algebraic expressions at $x=2$.

1. $-12 x+9+7 x-8$
2. $-5 x+1$

## THE COMMUTATIVE PROPERTIES

Let $a$ and $b$ represent real numbers, variables, or algebraic expressions.
Commutative Property of Addition:

Changing $\qquad$ when adding does not affect the $\qquad$ .

## Commutative Property of Multiplication:

Changing $\qquad$ when multiplying does not affect the $\qquad$ .

Example 3: Use the commutative property to write an algebraic expression equivalent to each of the following:

1. $2 x+4$
2. $x \cdot 13$

THE ASSOCIATIVE PROPERTIES
Let $a, b$, and $c$ represent real numbers, variables, or algebraic expressions. Associative Property of Addition:
$\qquad$ when adding does not affect the $\qquad$ .

## Associative Property of Multiplication:

Changing $\qquad$ when multiplying does not affect the $\qquad$ .

Example 4: Use the associative property to simplify the algebraic expressions:

1. $4 x+(7+x)$
2. $25(4 x)$

## THE DISTRIBUTIVE PROPERTY

Let $a, b$, and $c$ represent real numbers, variables, or algebraic expressions.

Multiplication $\qquad$ over $\qquad$ .

Example 5: Multiply:

1. $3(x+5)$
2. $-(4+x)$

OTHER FORMS OF THE DISTRIBUTIVE PROPERTY

| PROPERTY | MEANING | EXAMPLES |
| :--- | :--- | :--- |
| $a(b-c)$  <br> $=a b-a c$  <br>   <br>   <br> $a(b+c+d)$  <br> $=a b+a c+a d$  |  |  |
| $(b+c) a$ |  |  |
| $b a+c a$ |  |  |

## COMBINING LIKE TERMS

The $\qquad$ property lets us $\qquad$ and $\qquad$ like terms.

Example 6: Combine like terms:

1. $3(4 x)+(-x+21)$
2. $9 x+(x+5)-2(-x+11+3 y)$

## STEPS FOR SIMPLIFYING ALGEBRAIC EXPRESSIONS

1. Use the $\qquad$ property to remove $\qquad$ .
2. Rearrange terms and terms using the
and $\qquad$ properties. As you
hone your skills, you'll be doing this step mentally!
3. Combine $\qquad$ terms by combining the $\qquad$ of the $\qquad$ and keeping the same $\qquad$ .

## APPLICATIONS

The percentage of U.S. women, $W$, who used the internet $n$ years after 2000 can be modeled by the formula $W=2(2 n+25)+0.5(n+2)$.

1. Simplify the formula.
2. Use the simplified form of the mathematical model to find the percentage of U.S. women who used the internet in 2005.
