

Use elementary row or column operations to find the determinant.

$$3R_4 + R_3 \rightarrow R_3$$

$$R_1 + R_4 \rightarrow R_4$$

$$\begin{vmatrix} 4 & -7 & 6 & 1 \\ 9 & 2 & 7 & 0 \\ 3 & 9 & -3 & 3 \\ 0 & 7 & 4 & -1 \end{vmatrix} = \begin{vmatrix} 4 & -7 & 6 & 1 \\ 9 & 2 & 7 & 0 \\ 3 & 30 & 9 & 0 \\ 0 & 7 & 4 & -1 \end{vmatrix} = \begin{vmatrix} 4 & -7 & 6 & 1 \\ 9 & 2 & 7 & 0 \\ 3 & 30 & 9 & 0 \\ 4 & 0 & 10 & 0 \end{vmatrix}$$

$$\rightarrow = -1 \begin{vmatrix} 9 & 2 & 7 \\ 3 & 30 & 9 \\ 4 & 0 & 10 \end{vmatrix} \xrightarrow{C_2 \rightarrow C_3} = -(-1) \begin{vmatrix} 9 & 7 & 2 \\ 3 & 9 & 30 \\ 4 & 10 & 0 \end{vmatrix} \xrightarrow{-15R_1 + R_2 \rightarrow R_2} = \begin{vmatrix} 9 & 7 & 2 \\ -132 & -96 & 0 \\ 4 & 10 & 0 \end{vmatrix} = 2 \begin{vmatrix} -132 & -96 \\ 4 & 10 \end{vmatrix}$$

$$\begin{aligned} &= 2(-1320 + 384) \\ &= 2(-936) \\ &= \boxed{-1872} \end{aligned}$$