When you are done with your homework you should be able to ...

- $\pi~$ Distinguish between functions written in implicit form and explicit form
- $\pi~$ Use implicit differentiation to find the derivative of a function

Warm-up: Find the derivative of the following relations.

1. $x^2 + y^2 = 25$

2.
$$(y-1)^2 = -2(x+3)$$

IMPLICIT AND EXPLICIT FUNCTIONS

Up to this point, we have seen most functions expressed in ______ form.

Some functions are only _____ by an equation.

MATH 150/GRACEY

When you were differentiating the warm-up problems, you were able to explicitly write y as a function of x.

In the example above, it is difficult to write y as a function of x
______. In order to differentiate we must use
______ differentiation. T

Understand how to find $\frac{dy}{dx}$ implicitly, you must know which variable you are differentiating with respect to. You must use the ______ rule on any variable which is different than the one you are differentiating with respect to.

Example 1: Find the derivative of the following functions with respect to x. Simplify your result to a single rational expression with positive exponents. a. $y = x^5$

b.
$$y = y^5$$

c. $x^2 + y^2 = 25$

GUIDELINES FOR IMPLICIT DIFFERENTIATION

1. Differentiate both sides of the equation with respect to x.

2. Collect all terms involving $\frac{dy}{dx}$ on the left side of the equation and move all other terms to the right side of the equation.

3. Factor
$$\frac{dy}{dx}$$
 out of the left side of the equation.

4. Isolate
$$\frac{dy}{dx}$$
.

Example 2: Find the derivative of the following functions. Simplify your result to a single rational expression with positive exponents.

 $1. \quad 4\cos x \sin y = 1$

2.
$$x^2y + y^2x = -2$$

3.
$$x = \csc \frac{1}{v}$$

Example 3: Use implicit differentiation to find an equation of the tangent line to the hyperbola $\frac{x^2}{6} - \frac{y^2}{8} = 1$ at x = 1. Sketch the graphs of the hyperbola and the tangent line at x = 1.



Example 4: Find the points at which the graph of the equation $4x^2 + y^2 - 8x + 4y + 4 = 0$ has a horizontal tangent line.

Example 5: Find $\frac{\partial^2 y}{\partial x^2}$ in terms of x and y. 1 - xy = x - y