

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Solve the problem.**

1) Suppose that the dollar cost of producing  $x$  radios is  $c(x) = 400 + 20x - 0.2x^2$ . Find the marginal cost when 40 radios are produced. 1) \_\_\_\_\_

2) Assume that a watermelon dropped from a tall building falls  $y = 16t^2$  ft in  $t$  sec. Find the watermelon's average speed during the first 4 sec of fall and the speed at the instant  $t = 4$  sec. 2) \_\_\_\_\_

3) Does the graph of the function  $y = \tan x - x$  have any horizontal tangents in the interval  $0 \leq x \leq 2\pi$ ? If so, where? 3) \_\_\_\_\_

**Write the function in the form  $y = f(u)$  and  $u = g(x)$ . Then find  $dy/dx$  as a function of  $x$ .**

4)  $y = \cos^6 x$  4) \_\_\_\_\_

$$5) y = \tan\left(\pi - \frac{9}{x}\right)$$

5) \_\_\_\_\_

$$6) y = (-3x + 7)^5$$

6) \_\_\_\_\_

Find  $\frac{d^2y}{dx^2}$  for the given function.

$$7) y = 3 \cot\left(\frac{x}{10}\right)$$

7) \_\_\_\_\_

$$8) y = -2x^4(3x + 8)^2$$

8) \_\_\_\_\_

Find the value(s) of  $x$  for which the slope of the curve  $y = f(x)$  is 0.

$$9) f(x) = \frac{x - x^2}{2x^2 + 6}$$

9) \_\_\_\_\_

**Find the indicated derivative.**

10) Find  $y''$  if  $y = 6x \sin x$ .

10) \_\_\_\_\_

**Find the value(s) of  $x$  for which the slope of the curve  $y = f(x)$  is 0.**

11)  $f(x) = \frac{8x^2}{x^2 + 1}$

11) \_\_\_\_\_

**Find the derivative.**

12)  $s = 2t^2 + 7t + 4$

12) \_\_\_\_\_

**Find the derivative of the function.**

13)  $q = \sqrt{20r - r^7}$

13) \_\_\_\_\_

**Find the derivative.**

$$14) p = \frac{\sec q + \csc q}{\csc q}$$

14) \_\_\_\_\_

**Find the derivative of the function.**

$$15) g(x) = \frac{x^2 + 5}{x^2 + 6x}$$

15) \_\_\_\_\_

**Find the derivative.**

$$16) y = 6 - 3x^2$$

16) \_\_\_\_\_

$$17) y = \frac{2}{\sin x} + \frac{1}{\cot x}$$

17) \_\_\_\_\_

**Find the derivative of the function.**

18)  $f(t) = (6 - t)(6 + t^3)^{-1}$

18) \_\_\_\_\_

19)  $r = (\sec \theta + \tan \theta)^{-3}$

19) \_\_\_\_\_

**Provide an appropriate response.**

20) Find all points  $(x, y)$  on the graph of  $y = \frac{x}{(x - 7)}$  with tangent lines perpendicular to the line  $y = 7x - 2$ . 20) \_\_\_\_\_

21) Find an equation for the tangent to the curve  $y = \frac{27}{x^2 + 2}$  at the point (1, 9).

21) \_\_\_\_\_

22) The curve  $y = ax^2 + bx + c$  passes through the point (2, 8) and is tangent to the line  $y = 2x$  at the origin. Find a, b, and c.

22) \_\_\_\_\_

**The function  $s = f(t)$  gives the position of a body moving on a coordinate line, with  $s$  in meters and  $t$  in seconds.**

23)  $s = 5t^2 + 3t + 7, 0 \leq t \leq 2$

Find the body's speed and acceleration at the end of the time interval.

23) \_\_\_\_\_

Find the second derivative of the function.

$$24) y = \frac{x^4 + 7}{x^2}$$

24) \_\_\_\_\_

Given  $y = f(u)$  and  $u = g(x)$ , find  $dy/dx = f'(g(x))g'(x)$ .

$$25) y = \frac{1}{u^2}, u = 6x - 5$$

25) \_\_\_\_\_

$$26) y = \sin u, u = \cos x$$

26) \_\_\_\_\_

Find  $y'$ .

$$27) y = (x^2 - 2x + 2)(4x^3 - x^2 + 5)$$

27) \_\_\_\_\_

Find  $dy/dt$ .

$$28) y = \cos(\sqrt{8t + 11})$$

28) \_\_\_\_\_

Find  $y'$ .

$$29) y = \left(\frac{2}{x} + x\right)\left(\frac{2}{x} - x\right)$$

29) \_\_\_\_\_

Find  $dy/dt$ .

$$30) y = 5t(3t + 3)^4$$

30) \_\_\_\_\_



Find the second derivative.

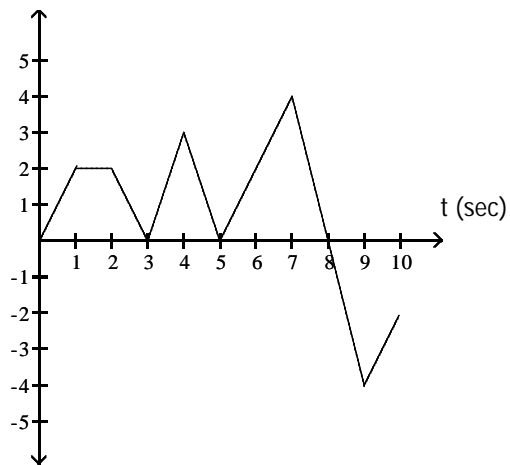
31)  $y = 8x^4 - 7x^2 + 7$

31) \_\_\_\_\_

The equation gives the position  $s = f(t)$  of a body moving on a coordinate line ( $s$  in meters,  $t$  in seconds).

32)  $s$  (m)

32) \_\_\_\_\_



When is the body moving forward?

Find an equation of the tangent line at  $x = a$ .

33)  $y = x - x^2$ ;  $a = 4$

33) \_\_\_\_\_

## Answer Key

Testname: M150\_2.1-2.4PRACTICE

- 1) \$4
- 2) 64 ft/sec; 128 ft/sec
- 3) Yes, at  $x = 0$ ,  $x = \pi$ ,  $x = 2\pi$
- 4)  $y = u^6$ ;  $u = \cos x$ ;  $\frac{dy}{dx} = -6 \cos^5 x \sin x$
- 5)  $y = \tan u$ ;  $u = \pi - \frac{9}{x}$ ;  $\frac{dy}{dx} = \frac{9}{x^2} \sec^2\left(\pi - \frac{9}{x}\right)$
- 6)  $y = u^5$ ;  $u = -3x + 7$ ;  $\frac{dy}{dx} = -15(-3x + 7)^4$
- 7)  $\frac{3}{50} \csc^2\left(\frac{x}{10}\right) \cot\left(\frac{x}{10}\right)$
- 8)  $-540x^4 - 1920x^3 - 1536x^2$
- 9)  $x = -3 \pm 2\sqrt{3}$
- 10)  $y'' = 12 \cos x - 6x \sin x$
- 11)  $x = 0$
- 12)  $4t + 7$
- 13)  $\frac{20 - 7r^6}{2\sqrt{20r - r^7}}$
- 14)  $\frac{dp}{dq} = \sec^2 q$
- 15)  $g'(x) = \frac{6x^2 - 10x - 30}{x^2(x + 6)^2}$
- 16)  $-6x$
- 17)  $y' = -2 \csc x \cot x + \sec^2 x$
- 18)  $f'(t) = \frac{2t^3 - 18t^2 - 6}{(6 + t^3)^2}$
- 19)  $\frac{-3 \sec \theta}{(\sec \theta + \tan \theta)^3}$
- 20)  $(0, 0)$ ,  $(14, 2)$
- 21)  $y = -6x + 15$
- 22)  $a = 1$ ,  $b = 2$ ,  $c = 0$
- 23) 23 m/sec, 10 m/sec<sup>2</sup>
- 24)  $\frac{d^2y}{dx^2} = 2 + \frac{42}{x^4}$
- 25)  $-\frac{12}{(6x - 5)^3}$
- 26)  $-\cos(\cos x) \sin x$
- 27)  $20x^4 - 36x^3 + 30x^2 + 6x - 10$
- 28)  $\frac{4}{\sqrt{8t + 11}} \sin(\sqrt{8t + 11})$
- 29)  $-\frac{8}{x^3} - 2x$
- 30)  $5(3t + 3)^3(15t + 3)$

## Answer Key

Testname: M150\_2.1-2.4PRACTICE

31)  $96x^2 - 14$

32)  $0 < t < 1, 3 < t < 4, 5 < t < 7, 9 < t < 10$

33)  $y = -7x + 16$